

Chapter12 IP weighting and marginal structures models

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The causal question

- Goal: Estimate the average causal effect of smoking cessation
A weight gain Y
- causal effect $:= E(Y^{a=1}) - E(Y^{a=0})$
- $E(Y^{a=1})$: mean weight gain that would have been observed if all individuals in the population had quit smoking before the follow-up visit

The causal question

- Average association effect $:= E(Y|A = 1) - E(Y|A = 0)$
- $L=(\text{sex,age,race,education,intensity and duration of smoking,physical activity in daily life, recreational exercise, weight})$: Confounder
- $E(Y^{a=1}) - E(Y^{a=0}) \neq E(Y|A = 1) - E(Y|A = 0)$
- We trying to adjust for these covariates with IP weighting

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Estimating IP weights via modeling

- IP weighting creates a pseudo-population in which the arrow from the covariates L to the treatment A is removed
- Pseudo-population has the following two properties
 - ① A and L are statistically independent
 - ② $E_{ps}(Y|A = a) = \sum_l E(Y|A = a, L = l)Pr(L = l)$

Estimating IP weights via modeling

- The individual-specific IP weights for treatment $W^A := \frac{1}{f(A|L)}$
- For Dichotomous treatment A , $f(A|L) = Pr(A = 1|L)$
- In section 2.4, We estimated $Pr(A = 1|L)$ nonparametrically
- In this chapter, we estimated $Pr(A = 1|L)$ with logistic regression model

Estimating IP weights via modeling

- 1 Estimate $Pr(A = 1|L)$ with logistic regression model
- 2 Create pseudo population by using IP weight
- 3 Estimate $E_{ps}(Y|A = 1) - E_{ps}(Y|A = 0)$ in pseudo population
- 4 If there is no confounding for the effect of A in the pseudo-population and the model for $Pr(A = 1|L)$ is correct, association is causation and an unbiased estimator of $E_{ps}(Y|A = 1) - E_{ps}(Y|A = 0)$ in the pseudo-population is also an unbiased estimator of $E(Y^{a=1}) - E(Y^{a=0})$ in the actual population

Estimating IP weights via modeling

- Estimating $E_{ps}(Y|A = 1) - E_{ps}(Y|A = 0)$ in the pseudo-population is to fit the linear mean model $E(Y|A) = \theta_0 + \theta_1 A$ by weighted Least square
- Find θ_0 and θ_1 such that minimize $\sum_{i=1}^n (\hat{W}_i (Y_i - \theta_0 - \theta_1 A))^2$ where $\hat{W}_i = \frac{1}{\hat{P}_r(A=1|L)}$ for quitter , $\hat{W}_i = \frac{1}{1 - \hat{P}_r(A=1|L)}$ for non-quitter

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Stabilized IP weights

- Stabilized IP weighing is another way to create a pseudo-population in which A and L are independent
- IP weights $W^A := \frac{1}{f(A|L)}$
- Stabilized IP weights $SW^A := \frac{f(A)}{f(A|L)}$

Stabilized IP weights advantages

- Stabilized IP weights have more narrow confidence interval range than IP weights
- Pseudo population made by stabilized IP weights would be of the same size as the study population

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Marginal structural models

- $E(Y^a) = \beta_0 + \beta_1 a$: Marginal structural mean model , where Y^a :counterfactual
- Causal effect $\beta_1 = E(Y^{a=1}) - E(Y^{a=0})$
- In pseudo population, fit $E(Y|A) = \theta_0 + \theta_1 A$
- In pseudo population, the association is causation
- So, $\hat{\theta}_1$ is consistent estimator of β_1